

Resonance Phenomena in the Habitable Zone caused by Giant Planets

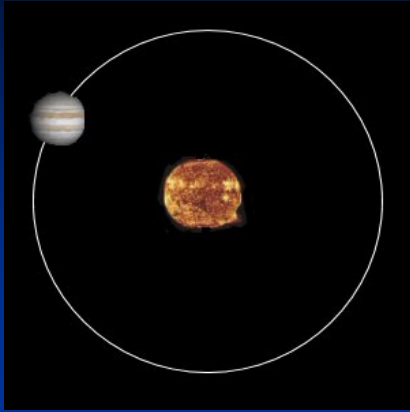
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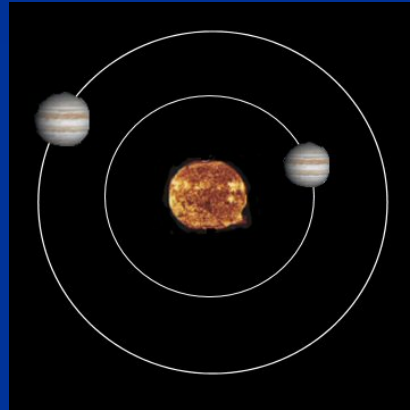
P. Robutel (IMCCE, Paris), A. Süli (Univ. of Budapest)

F. Freistetter (Univ. Jena)

Extra-solar planetary systems:



➤ **Single Star and Single Planet Systems**



➤ **Multi-planetary systems**

342 Extra-solar planets:

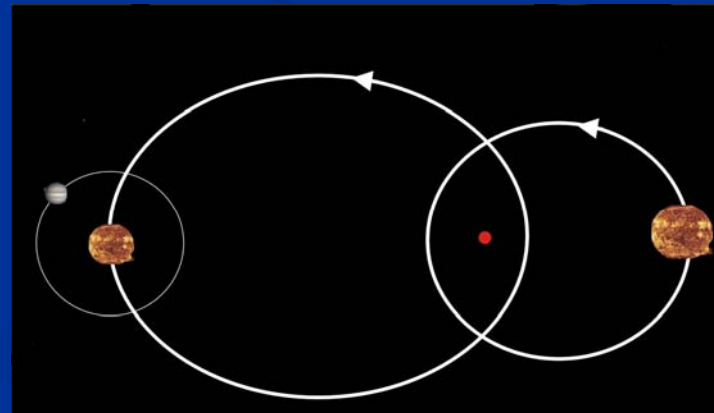
33 Multi-planet systems

1 system – 5 planets

1 system -- 4 planets

8 systems – 3 planets

23 systems – 2 planets



➤ **Binaries**

Why do we need stability studies?

(1) To be sure that a detected system is likely to exist

(2) Long-term stability of the planetary system is one of the basic requirements for the evolution of life on a terrestrial-like planet

Numerical Methods

Chaos Indicators:

Fast Lyapunov Indicator (FLI)

C. Froeschle, R.Gonczi, E. Lega
(1996)

(MEGNO – RLI – GALI --)

Lyapunov Exponent

Long-term numerical integration:

Stability-Criterion:

No close encounters within
the Hill's sphere

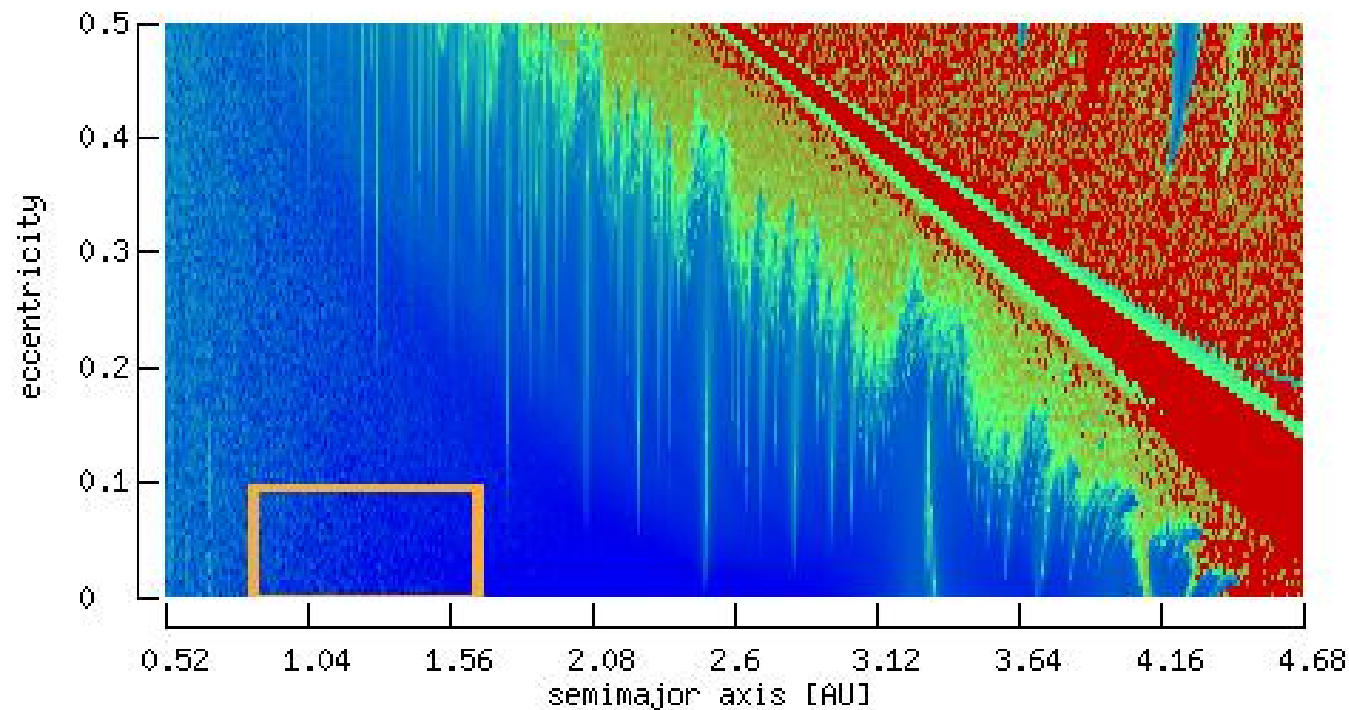
(i) Escape time

(ii) Study of the eccentricity:
maximum eccentricity

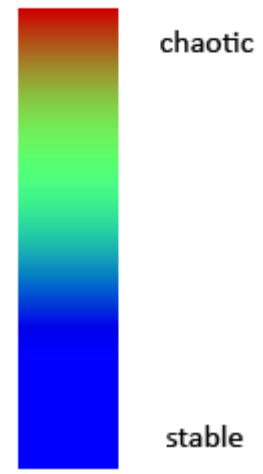
Stability of a terrestrial Planet in a Single-Star -- Single-Giant Planet System

Exocatalogue (Sandor et al., 2007)

ExoStab: <http://univie.ac.at/adg/exostab>



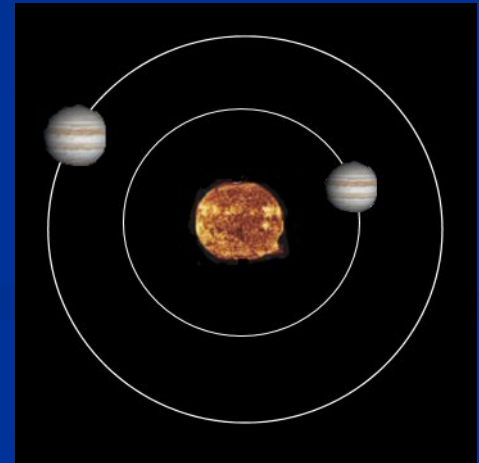
color code
for orbital motion



Multi-Planetary Systems

Dynamical classification (S.Ferraz-Mello, 2005)

- **Class Ia** → Planets in mean motion resonance
- **Class Ib** → Low-eccentricity near-resonant planet pairs
- **Class II** → Non-resonant planets with significant secular dynamics
- **Class III** → Hierarchical planet pairs



Initial Conditions and Computations

Jupiter: on its orbit

Saturn: $a_{\text{sat}} = 8 \dots 11 \text{ AU}$

$m_{\text{sat}} = 1 \dots 30 \times m_{\text{Sat}}$

Testplanets in the HZ:

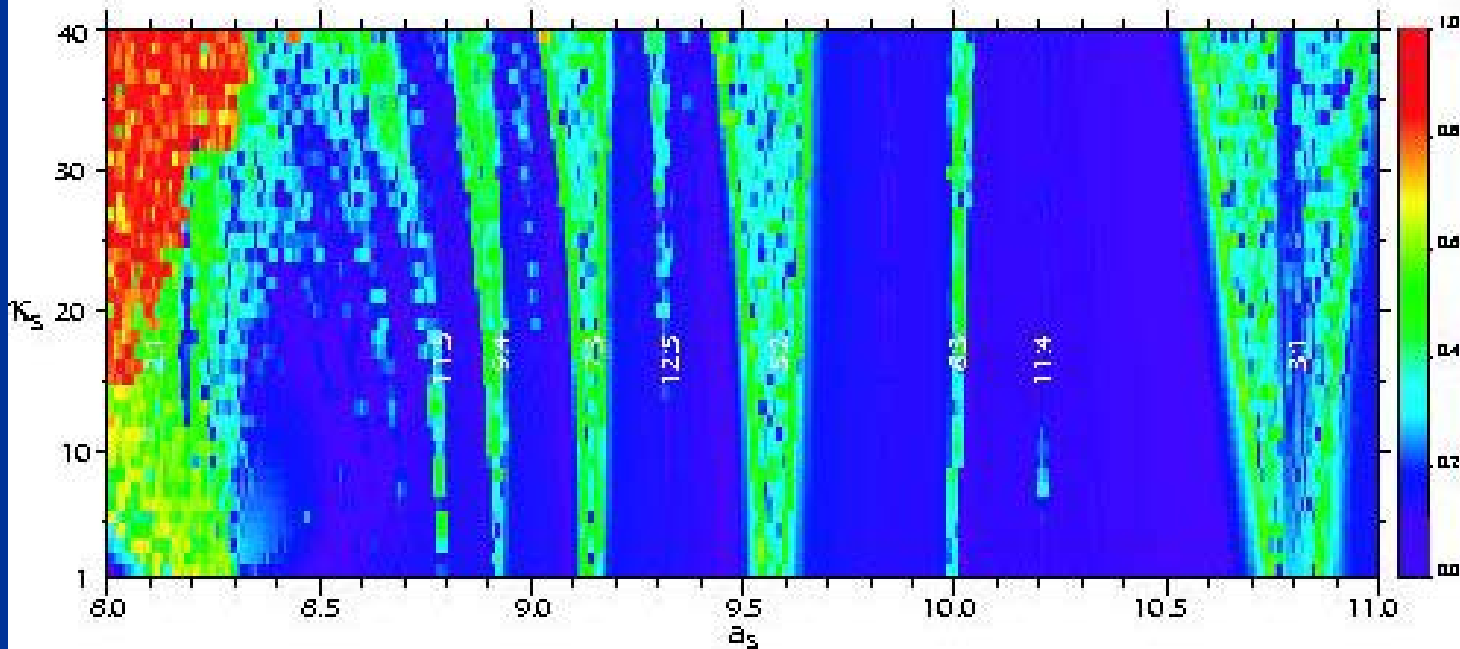
$a_{\text{tp}} = 0.6 \dots 1.6 \text{ AU}$

Mercury 6 (J. Chambers)

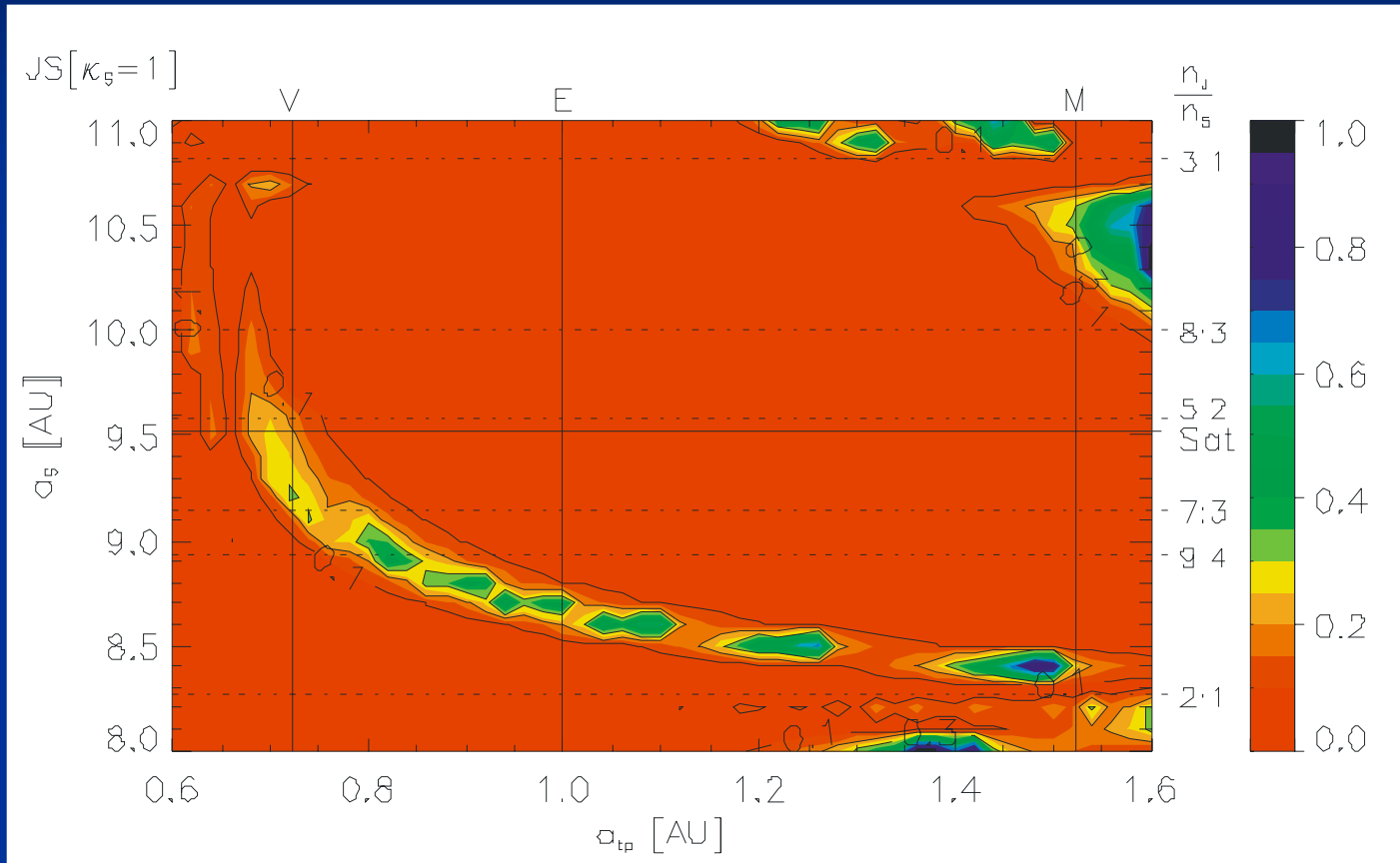
Integration time:
20 mio years

HZ: maximum ecc.

Mean Motion Resonances of Jupiter and Saturn



Perturbations of the HZ in the Sun – Jupiter – Saturn System:



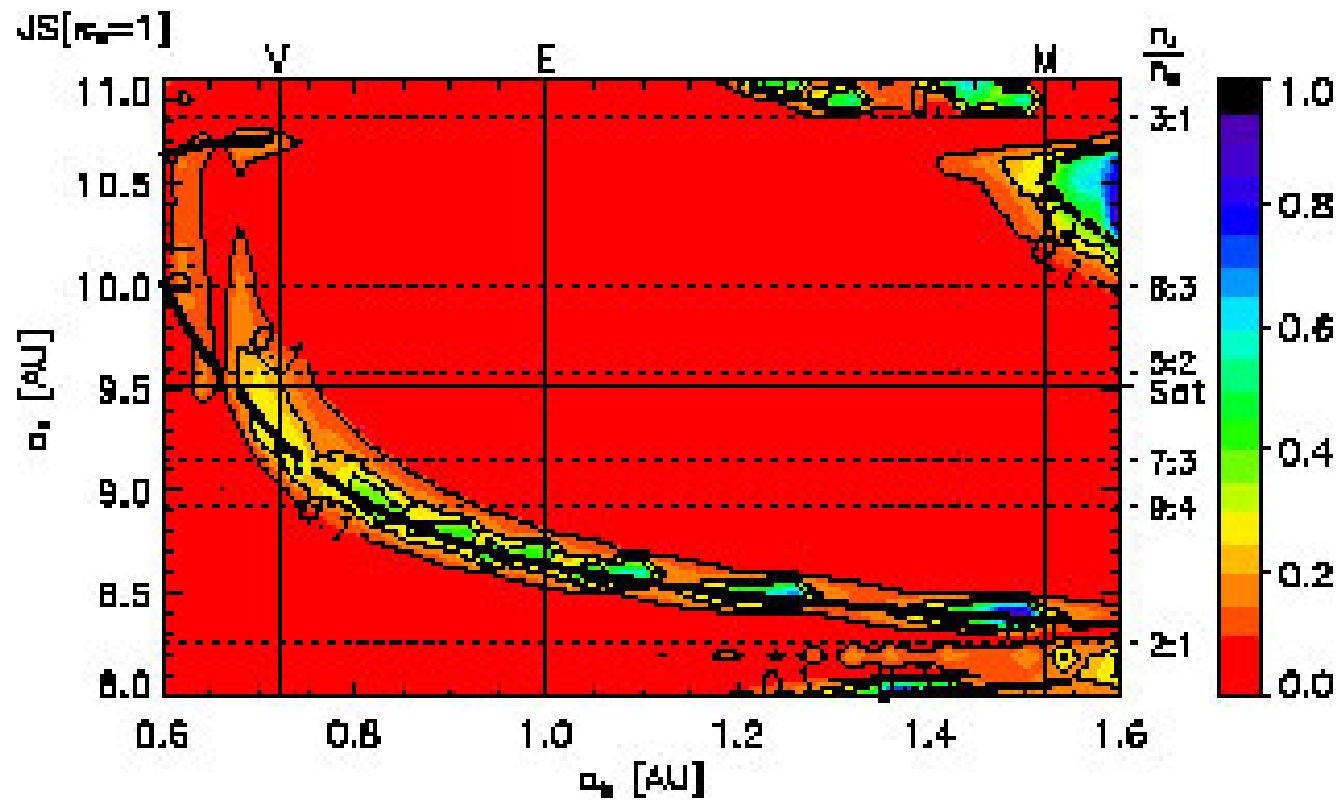
For details see Pilat-Lohinger et al., 2008, ApJ

HZ im Sonnensystem:

- Kasting: 0.93 – 1.3 AU
- Mischna: 0.93 – 1.7 AU
- Forget: 0.93 – 2 AU

$a < 0.93 \text{ AU}$ → H₂O becomes a major atmospheric compound and is rapidly lost to space after UV photolysis

$a > 1.3 \text{ AU}$ → CO₂ condensates in the atmosphere producing CO₂-clouds, that can affect significantly the T-CO₂ coupling



$$g = \frac{n}{4} \left(\frac{m_J}{M_{Sun}} \alpha_J^2 b_{3/2}^{(1)}(\alpha_J) + \frac{m_S}{M_{Sun}} \alpha_S^2 b_{3/2}^{(1)}(\alpha_S) \right)$$

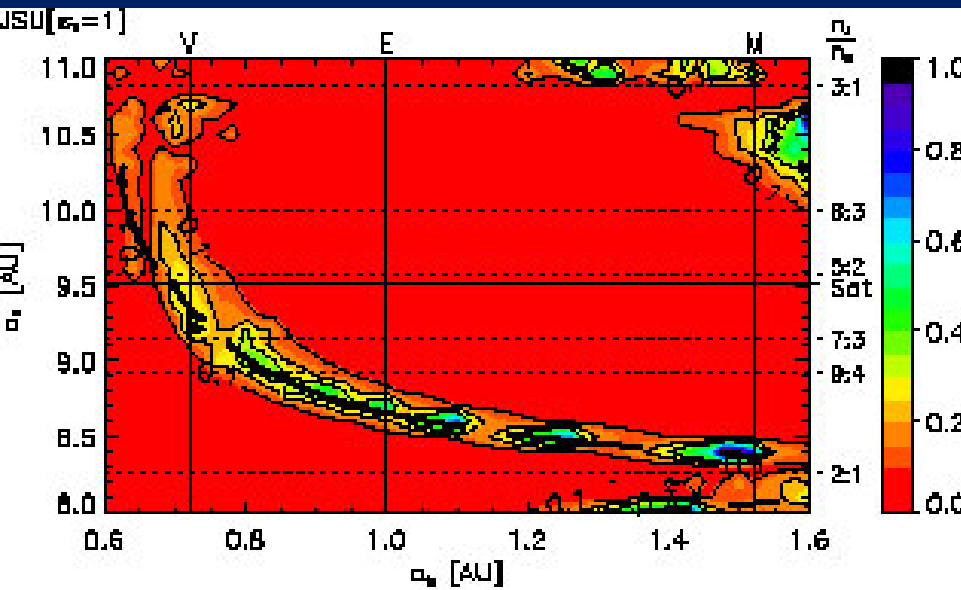
$$\alpha_J = \frac{a_{JJ}}{a_J}, \quad \alpha_S = \frac{a_{JS}}{a_S}$$

$b_{3/2}^{(1)}$ is a Laplace

HZ perturbed by 3 Giant Planets

(Jupiter, Saturn and Uranus)

Masses like in the Solar System

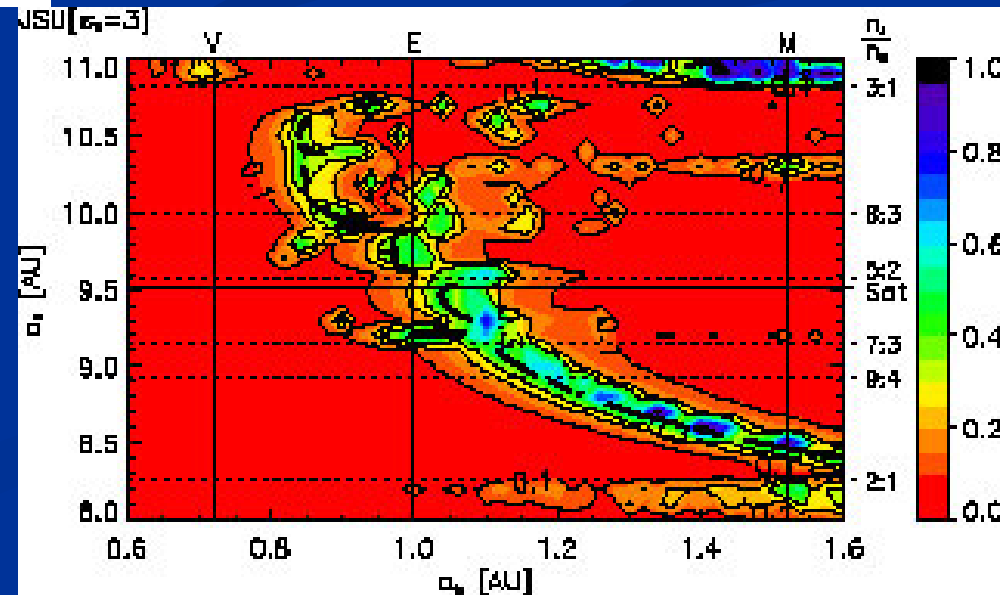


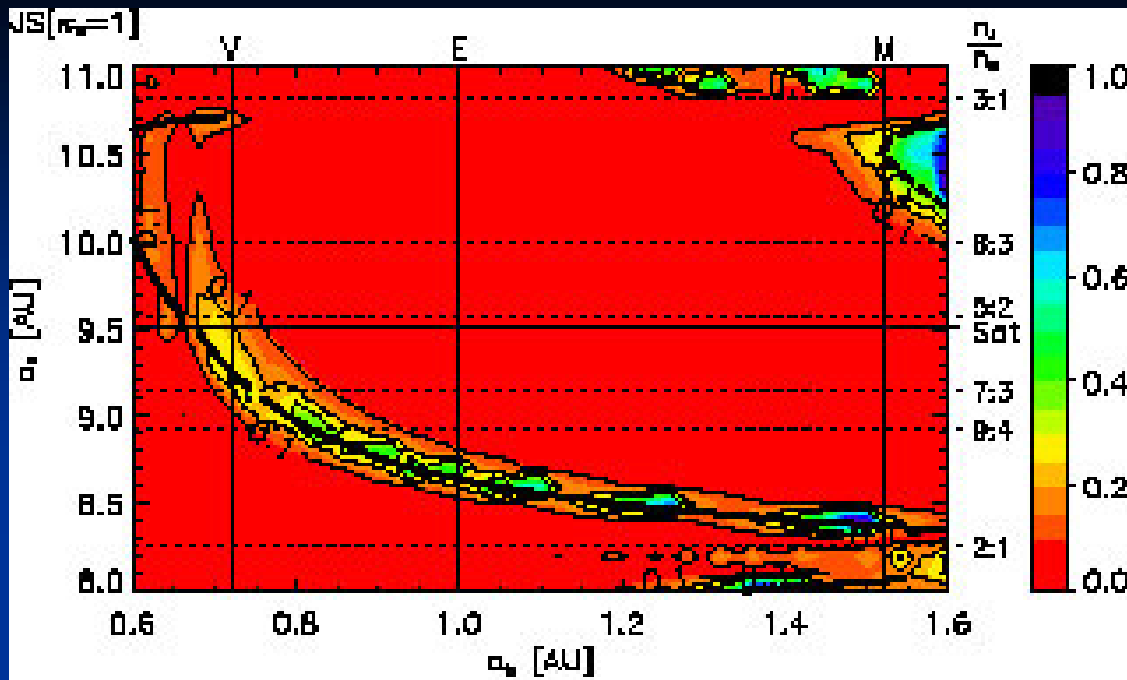
MMRs Saturn and Uranus:

5:2 at 10.4 AU

8:3 at 9.2 AU

larger Saturn mass:
(3 m_{Sat})

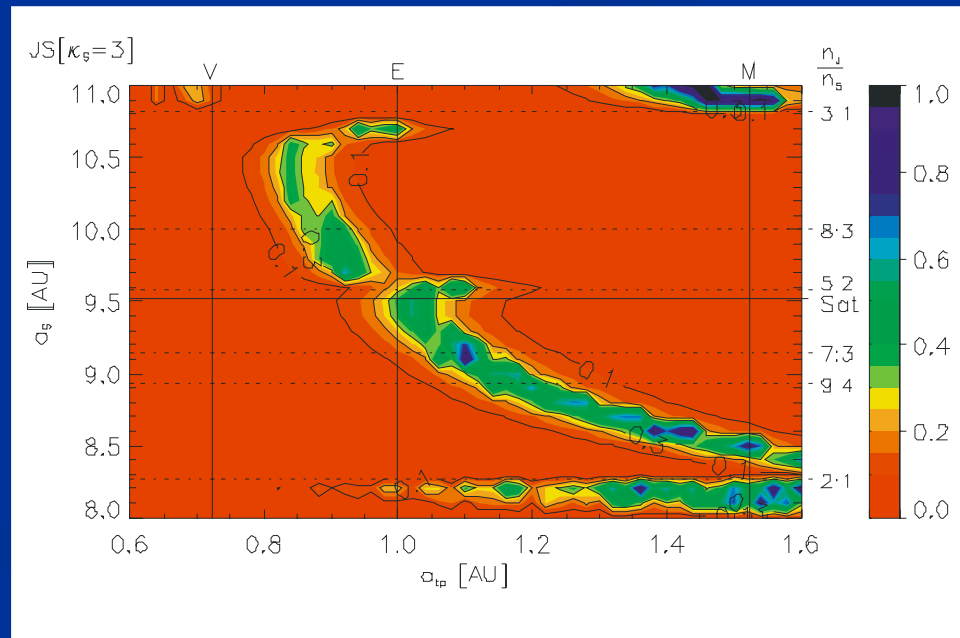




HZ perturbed by Jupiter and Saturn

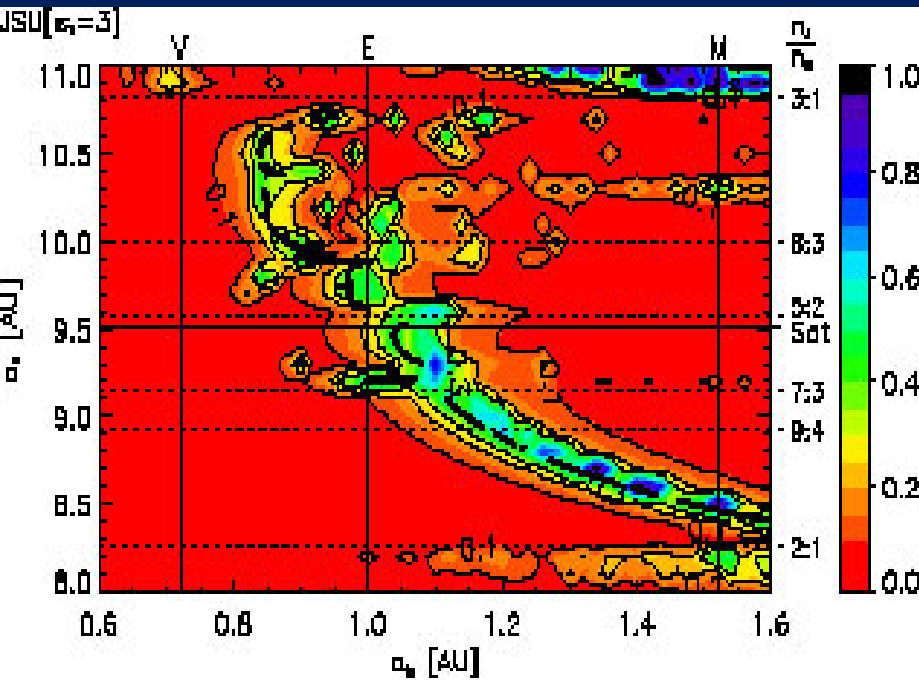
masses like in the
Solar System

larger Saturnmass
(3 mSat)



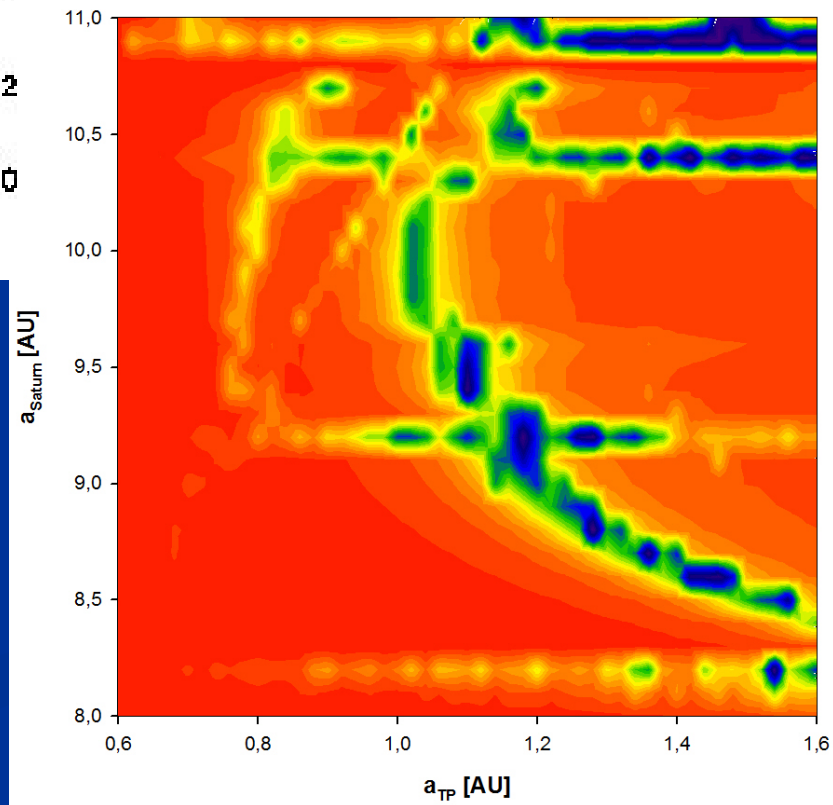
HZ perturbed by 3 Giant Planets

(Jupiter, Saturn and Uranus)



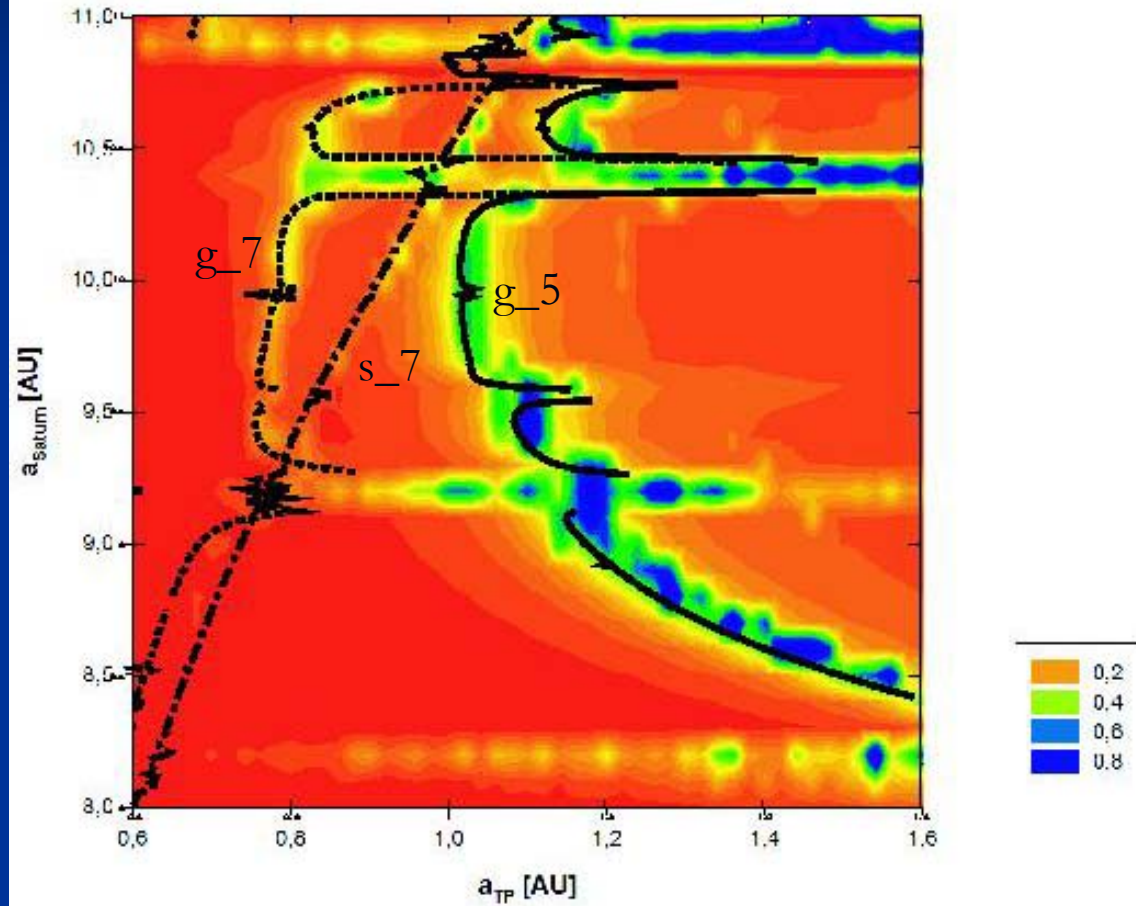
Larger Saturnmass

Sun - Jupiter - Saturn_(3m) - Uranus_(3m)

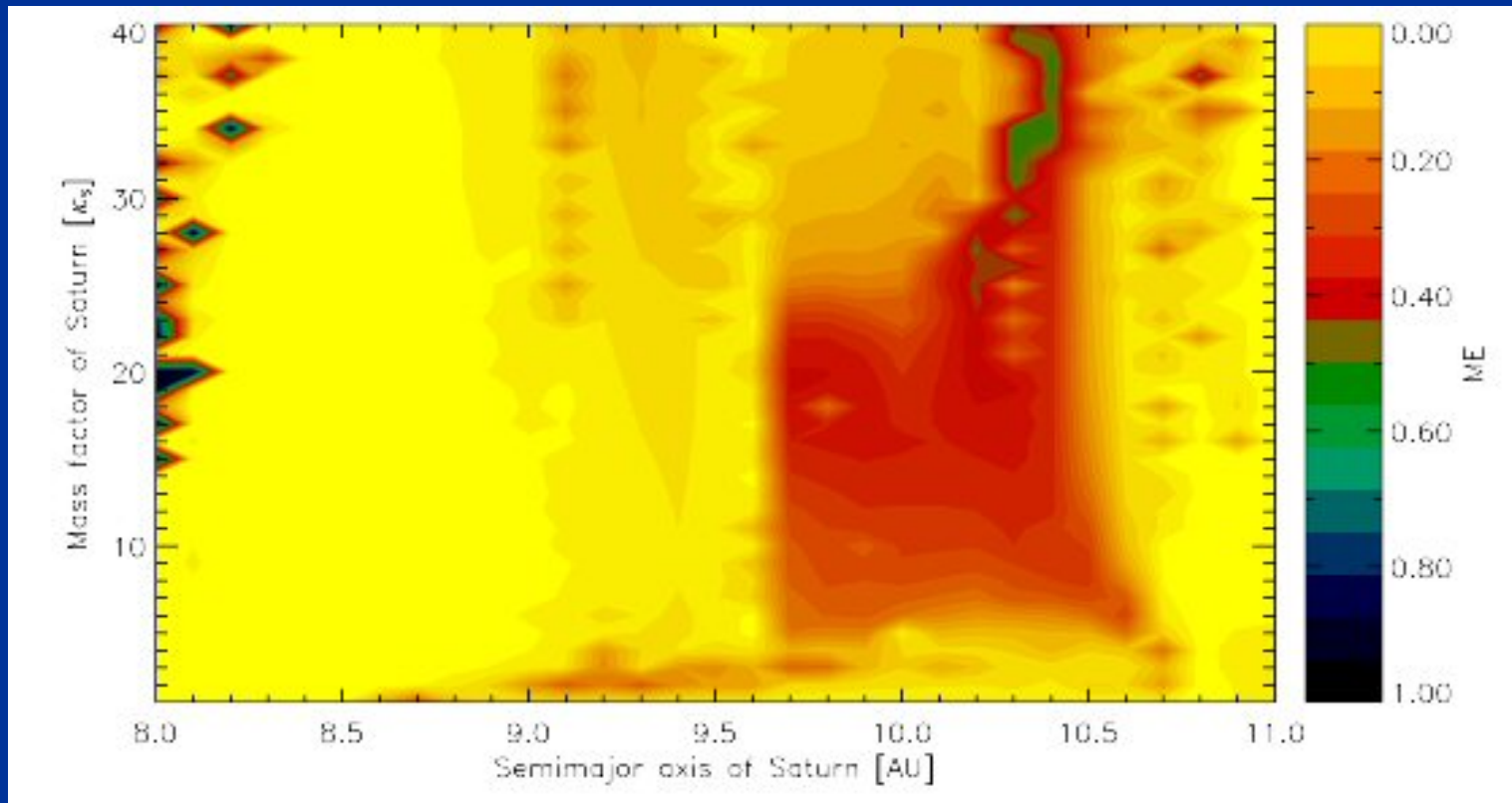


Larger Saturn- and Uranusmass

Sun - Jupiter - Saturn_(3m) - Uranus_(3m)

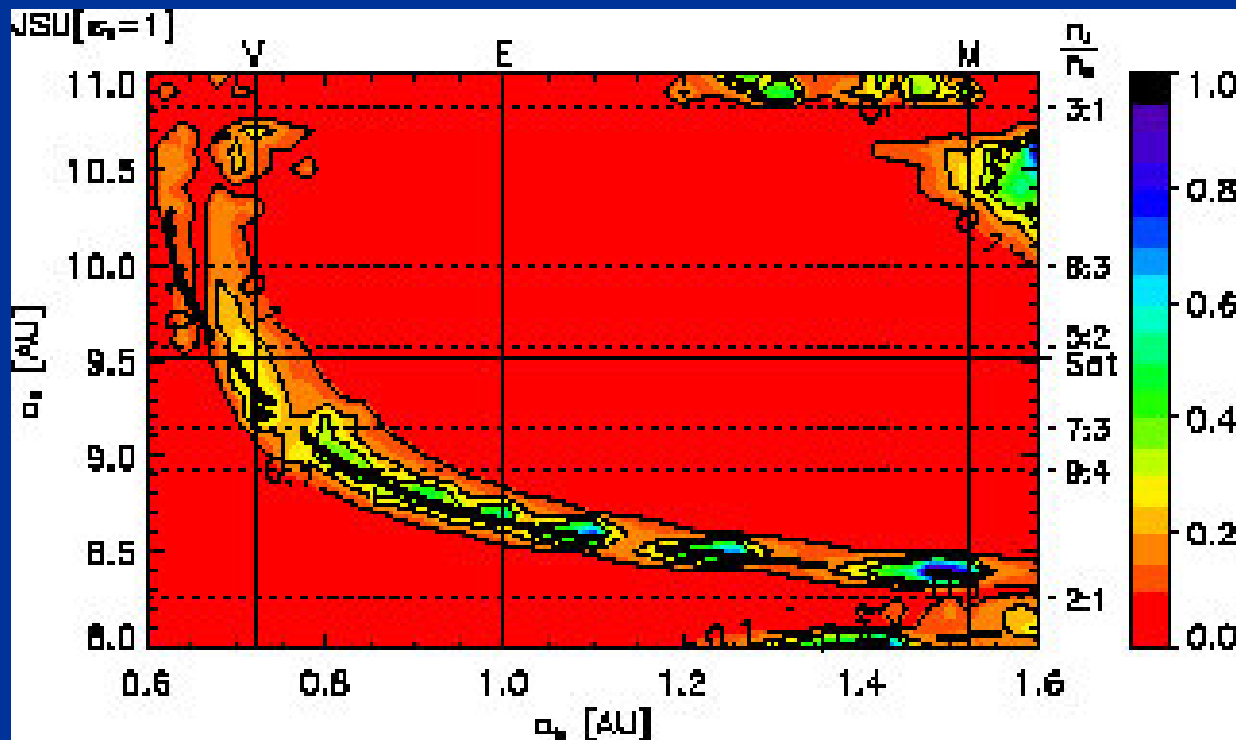


**Maximum eccentricity of an
Earth-like planet at 1 AU
for the different starting positions (x-axis) and
masses (y-axis) of Saturn**



Interesting Result:

The test-planet at Venus position has a maximum eccentricity > 0.2 for the Solar System parameters:

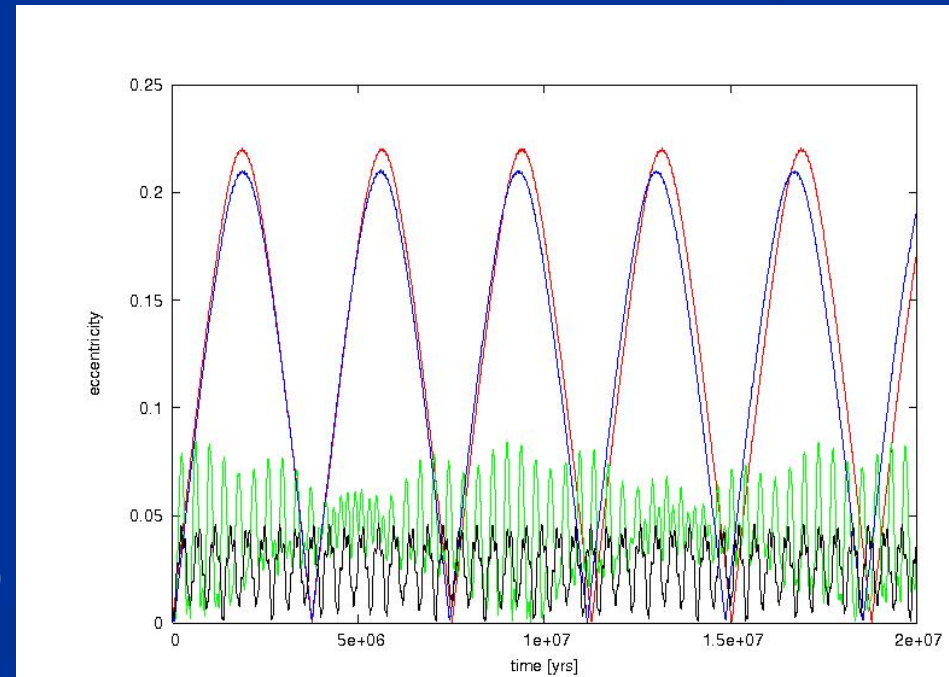
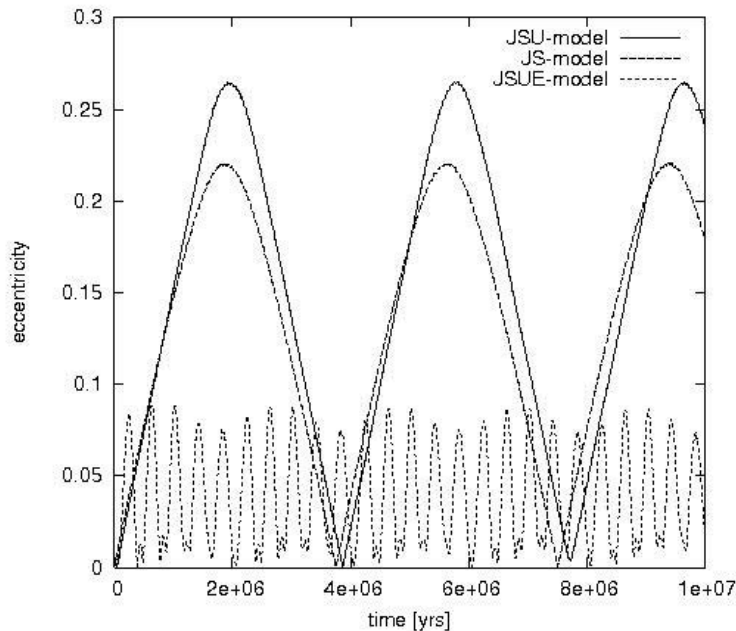


Time evolution of the eccentricity of a test-planet (e_{tp}) at Venus position:

JSU model = Jupiter-Saturn-Uranus model

JS model = Jupiter-Saturn model

JSUE model = Jupiter-Saturn-Uranus-Earth model

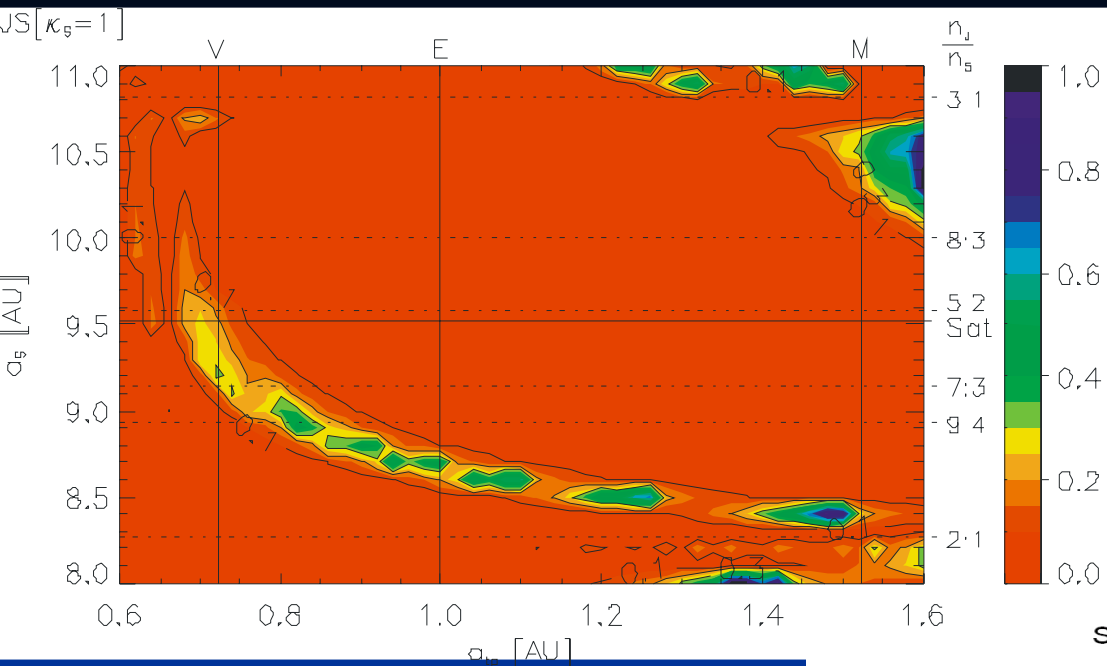


red line: e_{tp} in JS model ($m_{tp}=0$)

blue line: e_{tp} in JS model ($m_{tp}=m_{Venus}$)

green line : e_{tp} in JSE model ($m_{tp}=0$)

black line: e_{tp} in JSE model ($m_{tp}=m_{Venus}$)

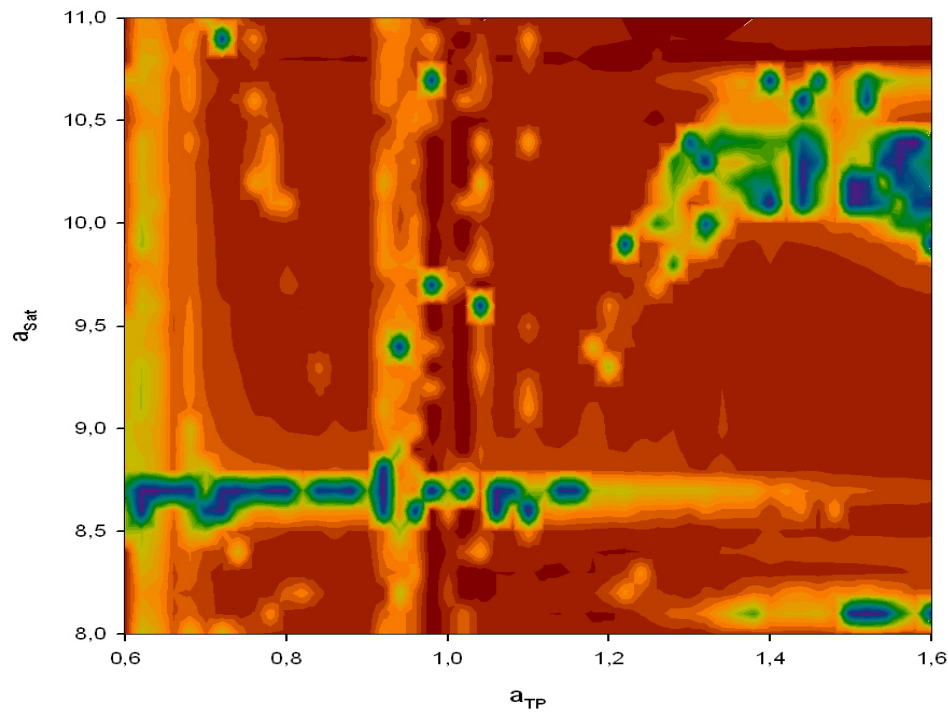


Perturbations of the HZ in two different dynamical models

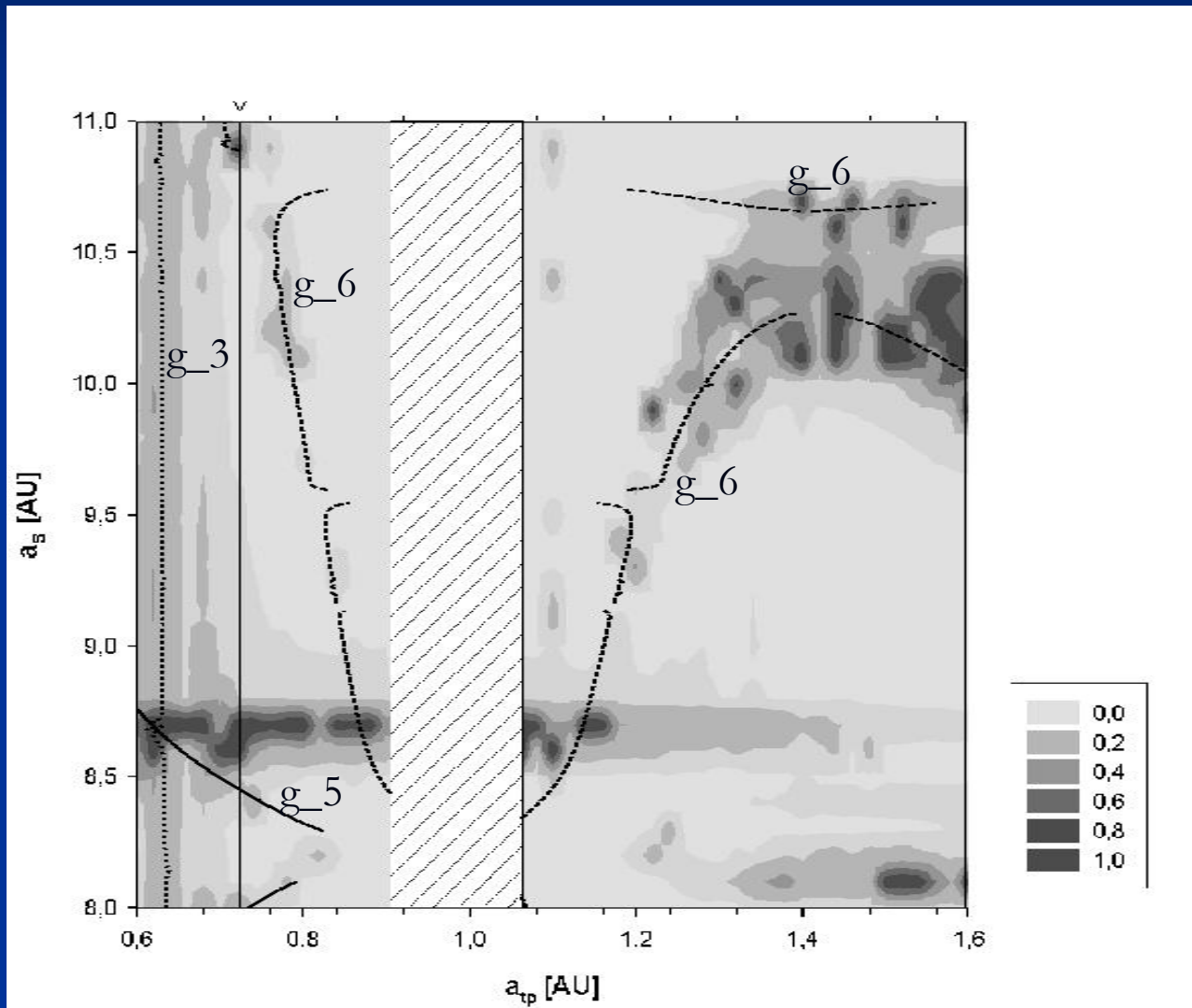
Sun - Jupiter - Saturn - Earth/Moon

Pilat-Lohinger, E., Süli, A., Robutel, P., Freistetter, F., 2008, ApJ, 681, p.1639

Pilat-Lohinger, E., Robutel, P., Süli, A., Freistetter, F., 2008, CeMDA, 102, p.83



Secular Perturbations of Jupiter, Saturn and Earth on the motion in the HZ:



Summary

- General stability studies are useful but only possible for simple systems like: detection of a small terrestrial planet in a **single-star single-planet** – **perturbations due to MMRs**
- In multi-planetary systems: secular perturbations occur in addition to the MMRs; both might lead to instabilities